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#### The Sources of Measured Agricultural Productivity Growth

**Robert G. Chambers** 

Selected Paper prepared for presentation at the International Agricultural Trade Research Consortium's (IATRC's) 2013 Symposium: Productivity and Its Impacts on Global Trade, June 2-4, 2013, Seville, Spain

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#### The Sources of Measured Agricultural Productivity Growth

Robert G. Chambers

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May 31, 2013

Bob Chambers Agricultural Productivity

# Fact 1: Aggregate US Agricultural Input and Output (1948-2008)



Source: Economic Research Service, United States Department of Agriculture

## Fact 2: US Agricultural TFP





#### Thinking about Facts 1 and Fact 2

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- Residual remains

### Fact 3: US Agriculture TFP Change (1949-2008)



Source: Computed from ERS/USDA official statistics

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$$\left(\frac{f(x_{t+1}, W_{t+1}, t+1)}{f(x_{t+1}, W_{t+1}, t)} \frac{f(x_t, W_t, t+1)}{f(x_t, W_t, t)}\right)^{\frac{1}{2}}$$

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• Instead we get:



• Incorporate stochastic nature of agriculture into productivity measurement, while allowing for inefficiency.

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$$T^{\Omega}\left(t
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 $g: \Omega \to \mathbb{R}_+$ ,  $\tilde{g} = (g(x, s_1, t), g(x, s_2, t), ....) \in \mathbb{R}^{\Omega}_+$  is a random variable.

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• Huge number of conceptual problems (Chambers and Quiggin, *ad nauseam*) but does have advantages: Implementable and easily comparable

#### Productivity Index

• Standard Malmquist-type productivity index:

$$\left(\frac{z^{0}}{g(x^{0},s^{1},t^{1})}\frac{g(x^{1},s^{1},t^{1})}{z^{1}}\right)^{\frac{1}{2}}\left(\frac{z^{0}}{g(x^{0},s^{0},t^{0})}\frac{g(x^{1},s^{0},t^{0})}{z^{1}}\right)^{\frac{1}{2}},$$

easily decomposes as

$$E^{s^{0},s^{1},t^{0},t^{1}}\left(z^{0},x^{0};z^{1},x^{1}\right)H^{s^{0},s^{1},t^{0},t^{1}}\left(z^{0},x^{0};z^{1},x^{1}\right),$$

and  $E^{s^0,s^1,t^0,t^1}(z^0,x^0;z^1,x^1)$  is a standard Färe et al. (1994) efficiency change index..

#### Productivity Index

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 H<sup>s<sup>0</sup>,s<sup>1</sup>,t<sup>0</sup>,t<sup>1</sup></sup> (z<sup>0</sup>, x<sup>0</sup>; z<sup>1</sup>, x<sup>1</sup>) is a combination of technical change and state of Nature change. Its decomposition is path dependent (standard problem, but see Henderson and Russell (2005))

$$H^{s^{0},s^{1},t^{0},t^{1}} = \Omega^{s^{0},s^{1}} \left( x^{0}, x^{1}, t^{0}, t^{1} \right) \times T^{t^{0},t^{1}} \left( x^{0}, s^{0}, x^{1}, s^{1} \right),$$

where  $\mathcal{T}^{t^0,t^1}\left(x^0,s^0,x^1,s^1\right)$  is technical change of the form

$$\left(\tilde{T}^{t^{0},t^{1}}\left(x^{0},s^{1}\right)\tilde{T}^{t^{0},t^{1}}\left(x^{0},s^{0}\right)\tilde{T}^{t^{0},t^{1}}\left(x^{1},s^{1}\right)\tilde{T}^{t^{0},t^{1}}\left(x^{1},s^{0}\right)\right)$$

and  $\Omega^{s^0,s^1}\left(x^0,x^1,t^0,t^1
ight)$  is state-contingent effect of the form

$$\left(\tilde{\Omega}^{s^{0},s^{1}}\left(x^{0},t^{0}\right)\tilde{\Omega}^{s^{0},s^{1}}\left(x^{0},t^{1}\right)\tilde{\Omega}^{s^{0},s^{1}}\left(x^{1},t^{0}\right)\tilde{\Omega}^{s^{0},s^{1}}\left(x^{1},t^{1}\right)\right)^{\frac{1}{2}}$$

#### **Operationally** speaking

•  $\Omega \subset \mathbb{R}^2_+$  defined empirically by observations on degree days between 8° and 32° C and precipitation

- $\Omega \subset \mathbb{R}^2_+$  defined empirically by observations on degree days between 8° and 32° C and precipitation
- Follow Banker and Morey (1986) and (implicitly) O'Donnell and Griffiths (2006) and approximate  $\hat{T}^{\Omega}(t)$  with CRS hull

$$\hat{T}^{\Omega}(t) = \left\{ \begin{array}{l} (z, x, s) : z \leq \sum_{k=1}^{48} \sum_{\nu=1}^{t} \lambda_{k\nu} z^{k\nu}, \\ x \geq \sum_{k=1}^{48} \sum_{\nu=1}^{t} \lambda_{k\nu} x^{k\nu}, \\ s = \sum_{k=1}^{48} \sum_{\nu=1}^{t} \lambda_{k\nu} s^{k\nu}, \\ \lambda_{k\nu} \geq 0 \end{array} \right\}$$

where the (x, z)' s are taken from V. Eldon Ball's state panel (1960-2004) and the s's from Schlenker and Roberts (2005)

### California Aggregate Output and Input (1960-2004)



Source: ERS/USDA

### Efficiency Change Index for California as calculated with and without Weather



#### California Productivity and H-Index: The Efficiency Residual Disappears



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- Too simple minded?
- For sure, but that's why I'm trying to raise the issue for the experts.