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**Market Equilibrium in the  
Presence of Green  
Consumers and Responsible  
Firms: A Comparative  
Statics Analysis**

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By **Nicola Doni**, Dipartimento Scienze  
Economiche, Università di Firenze

**Giorgio Ricchiuti**, Dipartimento  
Scienze Economiche, Università di  
Firenze

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By Nicola Doni, Dipartimento Scienze Economiche, Università di Firenze  
Giorgio Ricchiuti, Dipartimento Scienze Economiche, Università di Firenze

#### Summary

This paper analyzes how the interaction between green consumers and responsible firms affects the market equilibrium. The main result is that a higher responsibility by both producers and consumers can have different impacts on the efficiency of the firms' abatement activity, depending on the nature of the cleaning costs. When the abatement costs are fixed, the efficiency of the clean-up effort is always increasing in their degree of responsibility. On the other hand, when the abatement costs are variable, a higher level of responsibility may reduce social welfare. Finally, the first best allocation is never reached, even in the presence of the highest credible level of responsibility of both consumers and producers.

**Keywords:** Green Consumers, Corporate Social Responsibility, Vertical Differentiation

**JEL Classification:** D62, L13, L21

*We are grateful to the audience at the EARIE conference 2010 for the helpful comments and suggestions. We are also deeply indebted with Nicola Piana Agostinetti and Fabrizio Cipollini for their technical assistance to the numerical simulations. The usual disclaimer applies.*

*Address for correspondence:*

Nicola Doni  
Dipartimento Scienze Economiche  
Università di Firenze  
Via delle Pandette 9  
50127 Firenze  
Italy  
E-mail [nicola.doni@unifi.it](mailto:nicola.doni@unifi.it)

# Market Equilibrium in the Presence of Green Consumers and Responsible Firms: a Comparative Statics Analysis\*

Nicola Doni<sup>†</sup>      Giorgio Ricchiuti<sup>‡</sup>

February, 2011

## Abstract

This paper analyzes how the interaction between green consumers and responsible firms affects the market equilibrium. The main result is that a higher responsibility by both producers and consumers can have different impacts on the efficiency of the firms' abatement activity, depending on the nature of the cleaning costs. When the abatement costs are fixed, the efficiency of the clean-up effort is always increasing in their degree of responsibility. On the other hand, when the abatement costs are variable, a higher level of responsibility may reduce social welfare. Finally, the first best allocation is never reached, even in the presence of the highest credible level of responsibility of both consumers and producers.

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<sup>†</sup>Dipartimento Scienze Economiche, Università di Firenze, via delle Pandette 9, 50127 Firenze.  
E-mail nicola.doni@unifi.it

<sup>‡</sup>Dipartimento Scienze Economiche, Università di Firenze, via delle Pandette 9, 50127 Firenze.  
E-mail giorgio.ricchiuti@unifi.it

# 1 Introduction

In the late years a growing body of the environmental economics literature has been devoted to the analysis of the so called third generation instruments for the control of pollution. Indeed, the classic *command and control* approach can be substituted, or integrated, not only by economic instruments (as taxes, subsidies and tradable permits) but also by the voluntary market choices of environmentally aware agents.<sup>1</sup> However, the current debate is far from a complete understanding of the actual capabilities of individual and firm responsibility as a means to effectively promote environmental protection (see Bénabou and Tirole, 2010).

In many sectors firms try to increase their market share by advertising their production as environment-friendly. As noted by Kotchen (2005) and Besley and Ghatak (2007), environment-friendly goods can be viewed as impure public goods, in which private and public characteristics are bundled together. As emphasized by Bagnoli and Watts (2003), the form of this bundling can be explicit or implicit. The first case corresponds to situations in which firms improve the environmental quality of the good they provide and, consequently, they increase their marginal costs of production. On the other hand, the second case corresponds to situations in which firms sustain environmental programs whose benefits and costs are not proportional to their sales.

There is a large evidence that many consumers are willing to pay a price premium to purchase environment-friendly goods. The premium paid represents a form of voluntary contribution to the provision of a public good. In the economic literature there are different ways to reconcile this behavior with the traditional assumption of self-interested agents. A first attempt is based on the assumption that green consumers obtain a direct utility by the environmental qualities of the goods they buy. In this view green consumers derive a *warm glow* from their responsible action (Andreoni, 1990), due to social approval or to their internal moral motivation. On the other hand, we could think that green consumers behave as *conditional cooperator*, who accept to sacrifice their utility conditional on expectations that others will do the same. Indeed, many authors (e.g. Ostrom, 2000) emphasized that in the presence of social dilemmas, if all the individuals seek to maximize their egoistic interest, they are unavoidably trapped in a sub-optimal equilibrium. For this reason truly rational agents can choose to switch to more refined choice criteria. We do not deepen this problem in our paper, but when we carry out the welfare analysis we choose to explore only the influence

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<sup>1</sup>See Khanna, 2001, for a good survey on this historical evolution.

of responsible choices on the efficiency of the environmental protection activity, disregarding their consequences in terms of consumers' surplus. Indeed, the calculation of consumers' surplus requires a clear cut definition of consumers' utility.

The economic literature traditionally has analyzed the green consumers phenomenon in the framework of vertically differentiated markets. A first group of paper focused on how the presence of green consumers interacts with the optimal environmental policy (see Arora and Gangopadhyay, 1995; Cremer and Thisse, 1999; Moraga-Gonzalez and Padron-Fumero, 2002; Bansal and Gangopadhyay, 2003; Lombardini-Riipinen, 2005). A second group dealt with the impact of a higher consumers' consciousness on the market equilibrium and the associated social welfare. Frequently the results of these models warn against a naive confidence in consumers' responsibility as a solution to environmental problems. Indeed, rarely the market equilibrium in the presence of green consumers approximates the maximization of social welfare (see Eriksson, 2004; Conrad, 2005). Moreover, some authors showed that it cannot be taken for granted that a higher level of consumers' responsibility is always associate to less pollution and higher welfare<sup>2</sup> (Rodriguez-Ibeas, 2007; Garcia-Gallego and Georgantzis, 2009).

Our paper can be considered as an extension of the vertically differentiated duopoly put forward by Garcia-Gallego and Georgantzis (2009). They assume that consumers have a different willingness to pay (hereafter WTP) for "clean" products and they study how an increase in their aggregate WTP affects the market equilibrium. As far as the production technology is concerned, they assume that the costs and the benefits of the abatement activity are increasing and convex in the level of clean-up and independent of the level of production. This assumption covers the case in which firms devote lump-sum expenditures to environmental protection activities not directly associated to their production of the private good. However there are cases in which the benefits and the costs of the abatement activity are proportional to the quantity produced, as happens when firms improve the environmental quality of their production process.<sup>3</sup> So a first extension consists in repeating their analysis under a different assumption regarding the technology associated to the provision of the public good.

Moreover, the main novelty of our paper is that we allow firms to choose their

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<sup>2</sup>Similar conclusions are reached in a different framework by Calveras *et al.* (2007). They consider a model in which citizens first vote the minimum environmental standard and then buy a good produced in perfectly competitive markets. According to their analysis, a higher level of activism in the society may imply a higher level of pollution.

<sup>3</sup>Many existing models adopt this assumption. See for instance Cremer and Thisse (1999), Eriksson (2004), Lombardini-Riipinen (2005), Conrad (2005) and Rodriguez-Ibeas (2007).

market strategy in accordance with an objective function that may not coincide with profit maximization. Indeed, in some markets, especially when the good traded is an impure public good, we can observe competition between firms with different aims. For instance, standard for profit firms may compete with non-profit firms, whose main objective is the maximization of the positive externality associated to their production.<sup>4</sup>

Recently many firms spend a lot of efforts in order to persuade consumers that their behavior is socially responsible. However, there is not a general consensus with regard to the exact concept of corporate social responsibility (CSR). We report two polar definitions that can appear in sharp contrast.<sup>5</sup> According to a first point of view, a firm is socially responsible when it takes environment-friendly actions not required by law. In this light, CSR can be defined without any regard neither to the motivation of the firm's choices nor to the impact of such choices on the firm's profit. However, many authors believe that a firm is truly responsible only when it sacrifices its profit, at least in part, in order to carry out some social objective. Baron (2001) names the first behavior as *strategic* CSR and the second one as *altruistic* CSR.

In all the existing models regarding the influence of green consumers on the market equilibrium, firms are assumed to behave as standard profit maximizers. Consequently the current literature explores only the effect of the interaction between green consumers and firms engaged in strategic CSR. We propose a more general approach in which firms' objective function weighs together their profit and the social impact of their actions. In this view, firms' degree of CSR can be interpreted as the relative weight they assign to the second objective. Our purpose is to study the market equilibrium in the presence of green consumers and firms engaged in altruistic CSR. More specifically this work aims at analyzing

1. if a higher level of responsibility of both consumers and producers is always associated to a more efficient result in terms of pollution control;
2. if a full responsibility of both producers and consumers is sufficient to attain the first best level of pollution.

The remaining part of the paper is organized as follows: in Section 2 we present the general model and introduce the concepts of green consumers and

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<sup>4</sup>Becchetti and Huybrechts (2007) interpret in this way the Fair Trade sector.

<sup>5</sup>An interesting debate over this issue can be found in the first volume of the *Review of Environmental Economics and Policy*. In particular, see Lyon and Maxwell (2008) and Reinhardt et al. (2008).

responsible firms. In Section 3 we characterize the market equilibrium in the case in which the costs and the benefits of the cleaning technology are fixed (i.e.: independent of the quantity produced). In Section 4 we extend the same kind of analysis to the alternative case in which the costs and the benefits of clean-up are assumed to be proportional to the quantity produced. In both these sections we examine how changes in consumers' or firms' social responsibility affect the efficiency of the aggregate abatement activity in equilibrium. Section 5 concludes.

## 2 The general model

### 2.1 The technology

There is a physically homogeneous good, whose production generates pollution. The production costs depend on both the quantity produced,  $x$ , and the level of the abatement activity,  $e$ . Formally, the cost function for a generic firm  $i$  is:

$$C_i(e_i) = \frac{k}{2} e_i^2 x_i^\gamma, \quad \forall i = 1, \dots, n, \quad (1)$$

where  $k$  is a constant and  $\gamma$  indicates how the quantity produced affects the abatement costs. Specifically,  $\gamma$  can assume two values: zero when the abatement costs are fixed, and one when these costs are variable.

The total emissions for a single firm are:

$$Y_i(e_i) = \bar{e}x_i - e_i x_i^\gamma, \quad \forall i = 1, \dots, n; \quad (2)$$

$\bar{e}$  is the *unitary* level of emissions without clean-up activity. We assume that when the abatement costs are fixed,  $\gamma = 0$ , then the clean-up activity of a generic firm  $i$  is independent of  $x_i$ . In this case, according to the definition introduced by Bagnoli and Watts (2003), the private provision of the public good "abatement" is only implicitly linked to sales of the private good. On the other hand, when the abatement costs are variable,  $\gamma = 1$ , the clean-up activity of firm  $i$  is proportional to  $x_i$ . This case corresponds to a situation in which the provision of the public good and of the private good are explicitly linked. Finally, let us define  $Y = \sum_{i=1}^n Y_i$  the aggregate emissions.

### 2.2 The social welfare

Polluting emissions represent an externality, affecting negatively the consumers' utility. We normalize the consumers' population to a unit mass and we assume

that every unit of emission reduces the utility of a generic consumer by  $\rho$ , which is distributed according to  $F(\rho)$  over the support  $[0, \bar{\rho}]$ , where  $F(0) = 0$  and  $F(\bar{\rho}) = 1$ . As a consequence, the social benefits of the clean-up activity is equal to  $\rho^T E^T$  where  $E^T = \sum_{i=1}^n e_i x_i^\gamma$  is the total abatement and  $\rho^T = \int \rho dF(\rho)$  is its marginal social benefit.

We identify the social welfare  $W$  with the efficiency of the environmental protection. Consequently  $W$  is defined as the difference between the social benefits associated to the aggregate abatement activity and its total costs:

$$W = \sum_{i=1}^n \left[ \rho^T e_i - \frac{k}{2} (e_i)^2 \right] x_i^\gamma. \quad (3)$$

Hence, the maximization of the social welfare entails that the first best level of clean-up of each firm is:

$$e^{FB} = \frac{\rho^T}{k}, \quad \forall i = 1, \dots, n, \quad (4)$$

which does not depend on the quantity produced. It is worth noting that whatever the total abatement is, its cost effective allocation requires that firms' marginal costs coincide, implying that total abatement should be shared equally among them.

We assume that the environmental regulator cannot force firms to adopt a positive level of clean-up. Consequently, if  $\rho^T$  is strictly higher than 0, then the public good "abatement" is too scarce and responsible citizens can choose to voluntarily contribute to its provision by producing or consuming more environment-friendly goods.

### 2.3 The demand side

On the demand side, consumers are interested in buying only one unit of the good. Mainly, a share  $0 \leq \beta \leq 1$  of consumers' population (labeled as *green*) takes into account firms' abatement efforts in choosing which product to buy, while all the others consumers acts as (radical) free riders. We let the WTP of green consumers be heterogeneous among them. Formally, a generic green consumer chooses a product to maximize:<sup>6</sup>

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<sup>6</sup>We assume that each consumer takes the total emissions  $Y$  as exogenous because her individual contribution to pollution is negligible.



$$H = V - p + \theta e - \rho Y, \quad (5)$$

where  $V$  is the (homogeneous) gross utility of consuming one unit of the product and  $\theta$  is the individual WTP for the marginal increase in firms' abatement, assumed uniformly distributed in the interval  $[0, \bar{\theta}]$ .<sup>7</sup> Therefore the total WTP for more environment-friendly products,  $\theta^T$ , is equal to  $\frac{\beta \bar{\theta}}{2}$ . Let us define  $\mu$  as:

$$\mu = \frac{\theta^T}{\rho^T} = \frac{\beta \bar{\theta}}{2\rho^T}. \quad (6)$$

This ratio can be considered as an index of the social capital of the consumers' population because it represents how much their choices are driven by social rather than individualistic motivations. We limit the aggregate consumers' WTP to be lower than their aggregate marginal disutility of emissions, i.e.  $\theta^T$  is weakly lower than  $\rho^T$ . Given this assumption, it follows that  $0 \leq \mu \leq 1$ .

## 2.4 The supply side

On the supply side, following Garcia-Gallego and Georgantzis (2009), there is the coexistence of two kinds of firms. On the one hand, a fringe of firms who provide the good without employing any clean-up activity. Given that they sell an homogenous product and compete à la Bertrand, they charge a price equal to 0 (the marginal cost of production when  $e = 0$ ), and they do not achieve extra profit. On the other hand, in the presence of green consumers, other firms can choose to employ the cleaning technology in order to differentiate their product and to obtain a strictly positive profit. We assume that there are only two firms that are able to carry out this abatement activity. We use  $H$  and  $L$  to denote the variables associated to the firms choosing the *high* and the *low* level of abatement. Their profit is equal to:

$$\pi_i = p_i x_i - \frac{k}{2} e_i^2 x_i^\gamma, \quad i = L, H, \quad (7)$$

where  $x_i$  represents firm's  $i$  market share.

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<sup>7</sup>We choose to pay attention only to the case in which the lowest WTP is 0 in order to simplify our analysis of market equilibrium.

These two firms are labeled as *responsible* because they overcome the existing environmental regulation.<sup>8</sup> However they can have a different willingness to sacrifice their profit in order to increase their clean-up. Formally, we allow them to have the following composite objective function that weighs the maximization of their profit and the maximization of the positive externality associated to their abatement activity:

$$J_i = (\pi_i)^{1-\alpha_i} (\rho^T e_i x_i^\gamma)^{\alpha_i} \quad s.t. \quad \pi_i \geq 0, \quad i = L, H, \quad (8)$$

where  $\alpha_i \in [0, 1]$ . When  $\alpha_i = 0$  we have the standard case of a profit-maximizer firm; when  $\alpha_i = 1$  we have the opposite case of a non-profit firm who simply wants to maximize the positive impact of its clean-up under the constraint of non-negative profit.<sup>9</sup> In general, a responsible firm  $i$  pursues two different objectives simultaneously and  $\alpha_i$  is a parameter signaling the relative importance of the two criteria. More specifically,  $\alpha_i$  can be interpreted as a measure of the degree of (altruistic) CSR of firm  $i$ .<sup>10</sup>

## 2.5 Firms' competition

We model competition between the two responsible firms according to the usual framework adopted in duopoly models of vertical differentiation. There are two stages: in the first one, the two firms simultaneously choose the clean-up level, that can be defined as the (environmental) quality of their product. In the second

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<sup>8</sup>As sustained by Kotchen (2009), environment-friendly innovations are frequently introduced by eco-entrepreneurs where eco-entrepreneurship can be defined as "the practice of starting new businesses in response to an identified opportunity to earn a profit and provide a positive environmental externality". So, the assumption regarding the existence of only two responsible producers can be justified by noting that frequently innovation processes are driven by a limited number of firms. Further research will be devoted to the analysis of the case in which the number of responsible firms is endogenously determined by market competition.

<sup>9</sup>We assume that when  $\alpha_i = 1$  firm  $i$  maximizes the positive impact of its abatement activity also if its profit is equal to 0.

<sup>10</sup>As explained in De Donder and Roemer (2009), such objective can be interpreted as the weighted Nash bargaining solution of an efficient negotiation between two different factions inside the firm: one aiming at maximizing profit and the other aiming at maximizing the positive externality associated to firm's production. Such interpretation is correct if i) the no agreement pay-offs are  $(0, 0)$ , as happens when a firm is part of the competitive fringe, that does not obtain any extra-profit and does not produce any positive externality, ii) the objective function of each faction is log-concave in firm's strategic choices of  $p$  and  $e$  (for our case this property is proved in the technical appendix). According to such interpretation,  $\alpha_i$  represents the relative negotiation power of the faction supporting the abatement activity inside the firm  $i$ .

stage the two firms observe the choice of their competitor and simultaneously set the price. We know that when the lowest consumers' WTP is equal to 0, in equilibrium arises an uncovered market configuration (see Motta, 1993). This means that in equilibrium a group of green consumers buys a standard good from the competitive fringe.

The market share of each firm can be calculated by identifying  $\hat{\theta}$ , the indifferent consumer between purchasing from either the high or the low quality firm, and  $\bar{\theta}$ , the indifferent consumer between buying either the low or the null quality product. Straightforward algebra, using equation (5), it is easy to see that:  $\hat{\theta} = \frac{p_H - p_L}{e_H - e_L}$  and  $\bar{\theta} = \frac{p_L}{e_L}$ . As known, in a vertically differentiated duopoly, the high (low) quality firm sells to green consumers included in  $[\hat{\theta}, \bar{\theta}]$  ( $[\bar{\theta}, \hat{\theta}]$ ). Then each firm's market share is:

$$x_H = \frac{\beta}{\bar{\theta}} \left[ \bar{\theta} - \frac{p_H - p_L}{e_H - e_L} \right], x_L = \frac{\beta}{\bar{\theta}} \left[ \frac{p_H - p_L}{e_H - e_L} - \frac{p_L}{e_L} \right], x_0 = 1 - x_H - x_L, \quad (9)$$

where  $x_0$  is the total quantity sold by firms of the competitive fringe.

We apply the standard backward induction methodology by first analyzing the price equilibrium and then the environmental quality equilibrium. In the following sections we analyze separately the cases of fixed and variable costs.

## 3 Fixed Costs of Clean-up

### 3.1 The Market Equilibrium

In this section we study the case of variable costs of clean-up, i.e.  $\gamma = 0$ . By using equations (7) and (8) we can specify the objective function of the responsible firms as:

$$J_i = \left( p_i x_i - \frac{k}{2} e_i^2 \right)^{1-\alpha_i} \left( \rho^T e_i \right)^{\alpha_i} \quad s.t. \quad \pi_i \geq 0, \quad i = L, H. \quad (10)$$

It is worth noting that in case of fixed costs the generalization of the firms' objective function has no consequence on the price-setting stage. Indeed, at the second stage the abatement activity is considered as exogenous, and so the responsible firms choose their price strategy in order to maximize only their revenues, whatever their degree of CSR is. So the price equilibrium can be found by solving

simultaneously the revenue maximization of both firms. As shown in the existing literature (Motta, 1993; Arora and Gangopadhyay, 1995), at this stage the unique Nash equilibrium is characterized by the following equations:

$$p_H^* = 2\bar{\theta}e_H \frac{e_H - e_L}{4e_H - e_L},$$

$$p_L^* = \bar{\theta}e_L \frac{e_H - e_L}{4e_H - e_L},$$

yielding profits:

$$\pi_H = 4\beta\bar{\theta}e_H^2 \frac{(e_H - e_L)}{(4e_H - e_L)^2} - \frac{k}{2}e_H^2; \quad (11)$$

$$\pi_L = \beta\bar{\theta}e_H e_L \frac{(e_H - e_L)}{(4e_H - e_L)^2} - \frac{k}{2}e_L^2. \quad (12)$$

In order to identify the duopolists' maximization problem at the first stage, equations (11) and (12) are substituted in equation (10). The equilibrium levels of clean-up corresponds to the solutions that solve simultaneously<sup>11</sup> the following unconstrained<sup>12</sup> maximization problems:<sup>13</sup>

$$\begin{aligned} & \max_{e_H} \left[ 4\beta\bar{\theta}e_H^2 \frac{(e_H - e_L)}{(4e_H - e_L)^2} - \frac{k}{2}e_H^2 \right]^{1-\alpha_H} \left( \rho^T e_H \right)^{\alpha_H}; \\ & \max_{e_L} \left[ \beta\bar{\theta}e_H e_L \frac{(e_H - e_L)}{(4e_H - e_L)^2} - \frac{k}{2}e_L^2 \right]^{1-\alpha_L} \left( \rho^T e_L \right)^{\alpha_L}. \end{aligned}$$

The first order conditions require:

$$\frac{\partial J_H}{\partial e_H} = 0 \Leftrightarrow \beta\bar{\theta} \frac{4e_H^3 - (3 + 2\alpha_H)e_H^2 e_L + (2 - \alpha_H)e_H e_L^2}{(4e_H - e_L)^3} = \frac{2 - \alpha_H}{8} k e_H; \quad (13)$$

<sup>11</sup>As explained by Motta (1993), the solutions of this system are only the candidate equilibrium of the model. In the technical appendix we show that second order conditions hold, and consequently every solution represents effectively a local maximum. Moreover, we have checked that the firm choosing the high (low) quality has no incentive to "leapfrog" the rival firm and itself produce the lowest (highest) quality.

<sup>12</sup>We neglect the constrain that the firms' profit must be positive as we will verify that such condition is always satisfied in equilibrium.

<sup>13</sup>We use  $\alpha_H$  and  $\alpha_L$  to indicate the degree of CSR of the firms producing the *high* and the *low* level of clean-up. However, it is important to emphasize that we do not restrict the relative size of their degree of CSR.

$$\frac{\partial J_L}{\partial e_L} = 0 \Leftrightarrow \beta\bar{\theta} \frac{4e_H^3 - (7 - 2\alpha_L)e_H^2e_L + \alpha_L e_H e_L^2}{(4e_H - e_L)^3} = \frac{2 - \alpha_L}{2} k e_L. \quad (14)$$

In order to study whether firms' abatement activities are strategically substitutes or complements we have to investigate the sign of the following cross derivatives:

$$\frac{\partial^2 J_H}{\partial e_H \partial e_L} = 4\beta\bar{\theta} \frac{-8\alpha_H e_H^2 + (10 - 12\alpha_H)e_H e_L + (2 - \alpha_H)e_L^2}{(4e_H - e_L)^4}; \quad (15)$$

$$\frac{\partial^2 J_L}{\partial e_L \partial e_H} = \beta\bar{\theta} e_L \frac{(16 - 8\alpha_L)e_H^2 + (14 - 12\alpha_L)e_H e_L - \alpha_L e_L^2}{(4e_H - e_L)^4}. \quad (16)$$

Straightforward, the cross derivatives of each firm's objective function is decreasing in its own degree of CSR. However, the cross derivative of firm  $L$  (eq. 16) is always positive (given that  $\alpha_L \leq 1$ ): in equilibrium the optimal abatement for the low quality firm is always increasing in the abatement chosen by its rival. Conversely, the cross derivatives of firm  $H$  (eq. 15) is strictly positive for  $\alpha_H = 0$ , while is strictly negative when  $\alpha_H = 1$ . Hence, the best response of the high quality firm can be both increasing and decreasing in the abatement level chosen by its rival, depending on its degree of CSR (and on the equilibrium levels of firms' abatement).

Following the definition of Bulow *et al.* (1985), if  $\alpha_H$  is quite low, then  $e_H$  and  $e_L$  are strategic complements, while for higher values of  $\alpha_H$ , we have neither strategic complementarity nor strategic substitutability at the second stage because the slopes of the two reaction functions have different sign.

The solutions of the system given by equations (13) and (14) can be found making the ratio between them. We obtain:<sup>14</sup>

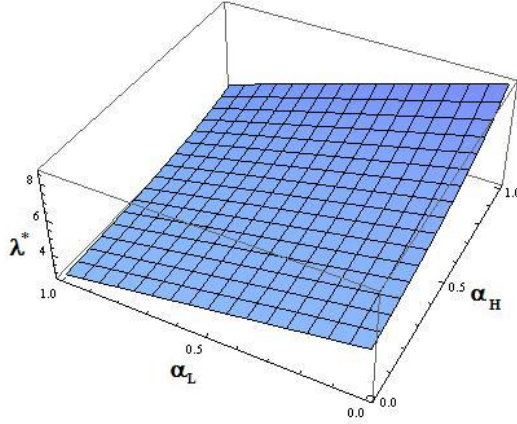
$$4(2 - \alpha_H)\lambda^3 - (46 - 20\alpha_L - 7\alpha_H + 2\alpha_L\alpha_H)\lambda^2 + (24 - 10\alpha_L + 16\alpha_H - 9\alpha_L\alpha_H)\lambda - 4(2 - \alpha_L)(2 - \alpha_H) = 0,$$

where  $\lambda$  is equal to  $\frac{e_H}{e_L}$ .  $\lambda$  can be interpreted as the degree of (environmental) differentiation. This equation has a unique acceptable solution  $\lambda^* = g(\alpha_H, \alpha_L)$ .

<sup>14</sup>This equation is a generalization of equation (7) of Motta (1993, p. 117) to the case in which firms aim at maximizing not only their profit but also the positive externality implicitly associated to their production.

In Figure 1 we show the three dimensional plot of  $\lambda^*$ . It is monotonically increasing (decreasing) in  $\alpha_H$  ( $\alpha_L$ ),  $\forall \alpha_H, \alpha_L \in [0, 1]$ : hence, the higher the degree of CSR of the firm  $H$  ( $L$ ) the higher (lower) the environmental differentiation. It's worth noting that  $\lambda^*$  has a maximum in  $g(1, 0) = 8, 6164$  and a minimum in  $g(0, 1) = 2, 7452$ .

Figure 1:  $\lambda^* = g(\alpha_H, \alpha_L)$



Substituting  $e_H$  with  $\lambda^*e_L$  in (14) we achieve the equilibrium level of clean-up of both firms as a function of  $\lambda^*$ ,  $\alpha_L$ ,  $\beta$ ,  $\bar{\theta}$ ,  $k$ :

$$e_L^* = \frac{2\beta\bar{\theta}}{(2 - \alpha_L)k} \frac{\lambda^*[4(\lambda^*)^2 - (7 - 2\alpha_L)\lambda^* + \alpha_L]}{(4\lambda^* - 1)^3};$$

$$e_H^* = \frac{2\beta\bar{\theta}}{(2 - \alpha_L)k} \frac{(\lambda^*)^2[4(\lambda^*)^2 - (7 - 2\alpha_L)\lambda^* + \alpha_L]}{(4\lambda^* - 1)^3}.$$

By recalling the equations (4) and (6) and rearranging we obtain:

$$e_L^* = \frac{4\mu\lambda^*[4(\lambda^*)^2 - (7 - 2\alpha_L)\lambda^* + \alpha_L]}{(2 - \alpha_L)(4\lambda^* - 1)^3} e^{FB}; \quad (17)$$

$$e_H^* = \frac{4\mu(\lambda^*)^2[4(\lambda^*)^2 - (7 - 2\alpha_L)\lambda^* + \alpha_L]}{(2 - \alpha_L)(4\lambda^* - 1)^3} e^{FB}. \quad (18)$$

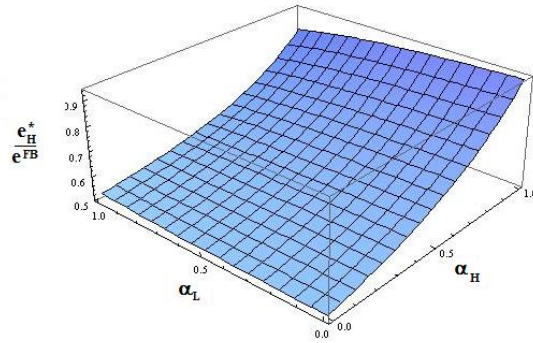
Trivially, if all consumers are radical free riders (i.e.:  $\mu = 0$ ), firms will not employ a cleaning technology, whatever their objective function is. It's worth

noting that in this model in order to have an abatement activity in equilibrium the presence of green consumers is both necessary and sufficient. On the other hand, the mere existence of responsible firms is not sufficient.

**Lemma 1.** *In the presence of green consumers (i.e.: if  $\mu > 0$ ),  $\forall \alpha_H, \alpha_L, \mu \in [0, 1], 0 < e_L^* < e_H^* < e^{FB}$ .*

*Proof.* In Figure 2 we report the ratio<sup>15</sup>  $e_H$  over  $e^{FB}$  calculated by means of equation (18). It can be easily seen that it is always positive but less than 1. Moreover, given that  $\lambda^*$  is always strictly higher than 1,  $e_L^*$  is always less than  $e_H^*$  for  $\mu > 0$ .

Figure 2:  $e_H^*/e^{FB}$



□

This lemma allows us to conclude that, even if consumers and producers were fully responsible, the market equilibrium will not correspond to the first best allocation: both the responsible firms never adopt an efficient level of clean-up. Moreover the allocation of the aggregate abatement is not cost-effective because in equilibrium the two responsible firms never adopt the same level of clean-up and so their marginal costs differ.

In order to analyze how the degree of responsibility of consumers and producers affects the overall efficiency of the abatement activity we can now conduct

<sup>15</sup>Figure 2 is plotted under the assumption that  $\mu = 1$ , so it indicates the maximum values that the ratio  $e_H$  over  $e^{FB}$  can assume.

some comparative statics. Note that given equations (17) and (18) there is a positive relationship between the social capital index and the equilibrium level of clean-up of both the responsible firms. The following lemma states how the degree of firms' social responsibility influences their equilibrium level of clean-up:

**Lemma 2.** *In the presence of green consumers (i.e.: if  $\mu > 0$ ):*

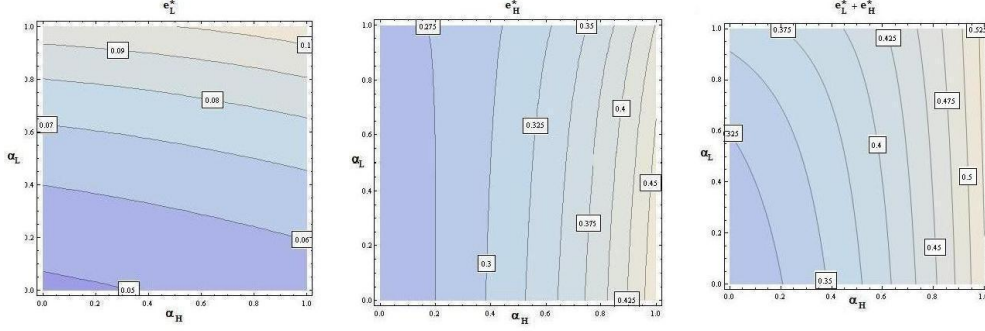
1.  $e_L^*$  is monotonically increasing in  $\alpha_L$  and  $\alpha_H$ ,  $\forall \alpha_H, \alpha_L \in [0, 1]$ ;
2.  $e_H^*$  is monotonically increasing in  $\alpha_H$ , while it is monotonically increasing (decreasing) in  $\alpha_L$  if  $\alpha_H$  is close to 0 (1). For intermediate values of  $\alpha_H$ ,  $e_H^*$  is not monotone in  $\alpha_L$ ;
3.  $E^{T*} = e_H^* + e_L^*$  is monotonically increasing in  $\alpha_L$  and  $\alpha_H$ ,  $\forall \alpha_H, \alpha_L \in [0, 1]$ .

*Proof.* The influence of the degree of CSR of both the responsible firms on their equilibrium levels of abatement are proved by means of the contour plots shown in Figure 3. The left-hand side shows that  $e_L^*$  has iso-curves negatively sloped and that it reaches its maximum value in the point  $(\alpha_H = 1, \alpha_L = 1)$ . This means that  $e_L^*$  is monotone increasing in both  $\alpha_H$  and  $\alpha_L$ . On the other hand, the central contour plot shows that the iso-curve of  $e_H^*$  are decreasing in correspondence of low values of  $\alpha_H$  and increasing for high values of  $\alpha_H$ . Moreover,  $e_H^*$  reaches its maximum value in correspondence of the point  $\alpha_H = 1, \alpha_L = 0$ . This prove that a higher  $\alpha_H$  always implies a higher  $e_H^*$ , while the influence of  $\alpha_L$  on  $e_H^*$  depends on the value of  $\alpha_H$ . Finally, the right-hand side shows that the sum of firms' abatement activities in equilibrium is monotone increasing in both  $\alpha_H$  and  $\alpha_L$ . Indeed, the iso-curves are negatively sloped and the maximum is reached in the point  $(\alpha_H = 1, \alpha_L = 1)$ . □

Therefore increments in the degree of responsibility of a firm always entails an increase of its own abatement activity. On the other hand increments in the degree of responsibility of the rival firm may not have a clear-cut effect for both firms. Indeed, it is always true that the higher  $\alpha_H$ , the higher  $e_L^*$ , while an increment of  $\alpha_L$  may both increase and decrease  $e_H^*$ , depending on the level of  $\alpha_H$ . This result is due to the different sign that the cross derivative of  $J_H$  can assume. As seen above, when firm  $H$  carries out a sufficiently high (low) degree of CSR, then its best response is decreasing (increasing) in the level of clean-up of firm  $L$ . As a consequence, given that an increment of  $\alpha_L$  increases  $e_L^*$ , we have that when  $\alpha_H$  is sufficiently high (low)  $e_H^*$  is decreasing (increasing) in  $\alpha_L$ . However, the total level of abatement is monotonically increasing in the degree of CSR of each firm.



Figure 3: Contour Plot of  $e_L^*$  and  $e_H^*$



Note: the lighter colors are associated with higher values.

### 3.2 The Social Welfare

In the case of fixed costs of clean-up, the social welfare defined in equation (3) can be rewritten as:

$$W = \sum_{i=H,L} \rho^T e_i^* - \frac{k}{2} (e_i^*)^2. \quad (19)$$

**Proposition 1.** *The social welfare is monotonically increasing in  $\mu$ ,  $\alpha_L$  and  $\alpha_H$ ,  $\forall \mu, \alpha_H, \alpha_L \in [0, 1]$ .*

*Proof.* We can write the variation of  $W$  with respect to a generic exogenous parameter  $z$  as:

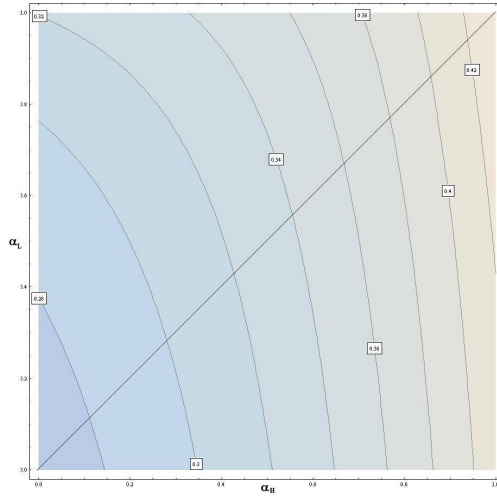
$$\frac{\partial W}{\partial z} = \sum_{i=H,L} (\rho^T - ke_i^*) \frac{\partial e_i^*}{\partial z}. \quad (20)$$

Given Lemma 1,  $e_i^* < e^{FB} \Leftrightarrow \rho^T - ke_i^* > 0$ . Therefore, the sign of the derivatives of the social welfare with respect to an exogenous parameter will depend only on how such parameter affects the equilibrium level of clean-up of both firms. If  $\frac{\partial e_i^*}{\partial z}$  has the same sign,  $\forall i = L, H$ , then also  $\frac{\partial W}{\partial z}$  will have that sign. Therefore, given equations (17) and (18) and Lemma 2, the social welfare is everywhere increasing in  $\mu$  and  $\alpha_H$ . As far as  $\alpha_L$  is concerned, rearranging equation 20 we obtain:

$$\frac{\partial W}{\partial z} = (\rho^T - ke_L^*) \frac{\partial E^{T*}}{\partial z} + k(e_H^* - e_L^*) \frac{\partial e_L^*}{\partial z}. \quad (21)$$

Applying Lemma 2 to formula 21 we can conclude that the social welfare is monotone increasing also in  $\alpha_L$ . The following contour plot (Figure 4) confirms that the social welfare has its global maximum in  $(\alpha_H = 1, \alpha_L = 1)$ .

Figure 4: Contour Plot of  $W(\alpha_H, \alpha_L)$



□

This result is in line with Garcia Gallego and Georgantzis (2009), who had already shown that, in the uncovered market configuration, the social welfare is increasing in consumers' WTP. However, in this paper we show that the social welfare is also increasing in the degree of CSR of both the responsible firms.

**Corollary 1.** *The highest social welfare is attained when  $\mu = 1$ ,  $\alpha_L = 1$  and  $\alpha_H = 1$ , but it does not correspond to the first best solution.*

*Proof.* Proposition 1 ensures that the maximum welfare associated to the market equilibrium is reached when both  $\mu$ ,  $\alpha_L$  and  $\alpha_H$  have their maximum value. In such case, the social welfare calculated by means of equation (19) is equal to  $0,4366 \frac{(\rho^T)^2}{k}$ . However, if the level of abatement of both the responsible firms was  $\frac{\rho^T}{k}$ , i.e. its first best level, then the social welfare would be equal to  $\frac{(\rho^T)^2}{k}$ .

Therefore in this case the social welfare attained in equilibrium is only the 43,66% of its first best level.  $\square$

Therefore, the market equilibrium never achieves the first best solution, even if both consumers and producers behave as fully responsible agents. The inefficiency of the market equilibrium is due to two different reasons: firstly, the clean-up of both the responsible firms is always lower than the first best level and consequently total abatement is below its optimal level. Moreover, the allocation of total abatement is not cost effective because it is not equally shared between the two responsible firms, whatever their degree of altruistic CSR (both these facts are emphasized in Lemma 1).

To sum up, when the clean-up activity of the responsible firms is only implicitly linked to their production, the efficient level of the abatement is never reached in equilibrium (Corollary 1). However, an increase of both firms' CSR and consumers' WTP have always a positive effect on the social welfare (Proposition 1). In the next section we shall show that even this result is not guaranteed when the clean-up activity is explicitly associated to the production level (i.e. when both benefits and costs of the cleaning technology are variable).

**Proposition 2.** *Assume that  $\alpha_H = \alpha'_L > \alpha_L = \alpha'_H$ ; then  $W(\alpha_H, \alpha_L) > W(\alpha'_H, \alpha'_L)$ ,  $\forall \alpha_H, \alpha_L \in [0, 1]$ .*

*Proof.* Let us analyze the contour plot of the Welfare (Figure 4). It is straightforward that if we consider both a point such that  $\alpha_H > \alpha_L$  and its symmetric point with respect to the 45° line, the former is always associated to a higher social welfare than the latter.  $\square$

The existing literature regarding vertically differentiated duopolies has already stressed the existence of two *symmetric* Nash equilibria at the quality stage. However, in the present model these two equilibria are *asymmetric* (if  $\alpha_H \neq \alpha_L$ ) given the asymmetry in the firms' objective functions. Proposition 2 states that the social welfare is always higher in the equilibrium in which the high quality firms is at the same time the firm with the highest degree of CSR.

Thanks to Propositions 1 and 2 we can compare a standard duopoly, where the firms are both profit maximizers, with a mixed duopoly, where a non-profit producer competes with a profit maximizer firm. When the costs of the abatement activity are only implicitly linked to the production level, then the presence of a non-profit firm is always welfare improving, and from the social welfare standpoint it is preferable the equilibrium in which the non-profit firm carries out the highest level of clean-up.

## 4 Variable Costs of Clean-up

### 4.1 The Market Equilibrium

In this section we study the case of variable costs of clean-up, i.e.  $\gamma = 1$ . Firms' objective function is:

$$J_i = (\pi_i)^{1-\alpha_i} (\rho^T e_i x_i)^{\alpha_i}, \quad i = L, H, \quad (22)$$

where:

$$\pi_i = \left( p_i - \frac{k}{2} e_i^2 \right) x_i, \quad i = L, H, \quad (23)$$

and the market shares of each firm are still given by (9). In this case the prices affect not only firms' profit but also the size of their positive externality. Therefore, equilibrium prices are now dependent on the degree of CSR of both firms.

By computing the first derivatives of  $J_H$  and  $J_L$  with respect to prices and then solving the system we obtain the following equations for the equilibrium prices:

$$p_H^* = \frac{e_H [(2 - \alpha_L) k e_H^2 + (1 - \alpha_H) k e_L^2 + 2\bar{\theta}(1 - \alpha_H)(2 - \alpha_L)(e_H - e_L)]}{2[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]},$$

$$p_L^* = \frac{e_L [(1 - \alpha_L) k e_H^2 + (2 - \alpha_H) k e_L e_H + 2\bar{\theta}(1 - \alpha_H)(1 - \alpha_L)(e_H - e_L)]}{2[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]},$$

yielding profits:

$$\pi_H = (1 - \alpha_H)(e_H - e_L) x_H^2 \frac{\bar{\theta}}{\beta}, \quad (24)$$

$$\pi_L = (1 - \alpha_L)(e_H - e_L) \frac{e_L}{e_H} x_L^2 \frac{\bar{\theta}}{\beta}, \quad (25)$$

where:

$$x_H = \frac{\beta e_H [(2 - \alpha_L)(2\bar{\theta} - k e_H) - k e_L]}{2\bar{\theta}[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]}, \quad (26)$$

$$x_L = \frac{\beta e_H [(1 - \alpha_H)(2\bar{\theta} - k e_L) + k e_H]}{2\bar{\theta}[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]}. \quad (27)$$

We can now include equations (24) and (25) in the generic equation (22) and derive the first order conditions of the first stage obtaining the following system of equations:

$$\frac{\partial J_H}{\partial e_H} = 0 \Leftrightarrow (2 - \alpha_H)(e_H - e_L) \frac{\partial x_H}{\partial e_H} + \frac{e_H - \alpha_H e_L}{e_H} x_H = 0; \quad (28)$$

$$\frac{\partial J_L}{\partial e_L} = 0 \Leftrightarrow (2 - \alpha_L)(e_H - e_L) \frac{e_L}{e_H} \frac{\partial x_L}{\partial e_L} + \frac{e_H - 2e_L + \alpha_L e_L}{e_H} x_L = 0. \quad (29)$$

Moorthy (1988) has already shown that when vertically differentiated firms behave as profit maximizers, their reaction functions are both positively sloped and so their quality choices are strategic complements. However, it is easy to check that if the high quality firm is a non-profit firm, i.e. when  $\alpha_H = 1$ , its best response function is negatively sloped<sup>16</sup> while the best response function of firm  $L$  is still positively sloped. Therefore we may not record neither strategic complementarity nor strategic substitutability, as in the fixed costs case.

The system given by equations (28) and (29) can have at maximum one acceptable solution (i.e.: such that  $e_H^* \geq e_L^*$ ). When one solution exists, such solution corresponds to the equilibrium levels of marginal clean-up of both firms<sup>17</sup>, which depend on the parameters  $\alpha_H$  and  $\alpha_L$ . The solutions in the closed form are not analytically feasible. However, some clear results emerges when one of the duopolists is a non-profit firm and it produces either the high-quality or the low-quality good.

**Proposition 3.** *If  $\alpha_L = 1$ , then at the first stage no Nash equilibrium exists.*

*Proof.* In this case the market shares of the responsible firms can be rewritten by substituting  $\alpha_L = 1$  in formula (26) and (27). We obtain:

$$x_H = \frac{\beta(2\bar{\theta} - ke_L - ke_H)}{2\bar{\theta}(2 - \alpha_H)}, \quad (30)$$

<sup>16</sup>Indeed, in such case the cross derivative of the objective function of firm  $H$  is equal to  $-\frac{\beta k}{2\bar{\theta}(2 - \alpha_L)}$ .

<sup>17</sup>In the technical appendix it is shown that in correspondence of the unique acceptable solution second order conditions hold also in the case of variable costs. However, not all the candidate solutions are valid because, as reported in the technical appendix, in some cases some firm has an incentive to leapfrog the "equilibrium" level of marginal abatement of its rival.

$$x_L = \frac{\beta[(1 - \alpha_H)(2\bar{\theta} - ke_L) + ke_H]}{2\bar{\theta}(2 - \alpha_H)}. \quad (31)$$

The derivatives of  $J_L$  with respect to  $e_L$  is equal to:

$$\frac{\partial J_L}{\partial e_L} = e_L \frac{\partial x_L}{\partial e_L} + x_L = 2(1 - \alpha_H)(\bar{\theta} - ke_L) + ke_H \quad (32)$$

From equation ((30)) we can deduce that  $x_H \geq 0 \Leftrightarrow ke_L \leq \bar{\theta}$ . This fact implies that equation ((32)) is always strictly positive. Consequently, at the first stage the firm  $L$  wants to choose  $e_L = e_H$ , the maximum level of marginal abatement under the constraint that  $e_L$  must be weakly lower than  $e_H$ . On the other hand, if  $\alpha_H < 1$ , the firm  $H$  always want to choose  $e_H > e_L$ , because if  $e_H = e_L$  its profit is equal to 0. Hence, when  $\alpha_L = 1$  no Nash equilibrium exists at the first stage.  $\square$

Therefore, when one of the two responsible producers is a non-profit firm, there is no equilibrium in which it chooses the low level of marginal abatement. Indeed, in such case the firm  $L$  would mimic the choice of its competitor, while the firm  $H$  would choose a level of marginal abatement strictly higher than the level of its rival.

As a consequence, in the presence of a non-profit firm, the only Nash equilibrium can be characterized by substituting  $\alpha_H = 1$  in equations ((28)) and ((29)).

**Lemma 3.** *If  $\beta > 0$ ,  $\bar{\theta} > 0$ , and  $\alpha_H = 1$ , then in equilibrium:*

1.  $e_L^*$  is monotonically increasing in  $\bar{\theta}$  and  $\alpha_L$ , decreasing in  $k$  and independent of  $\beta$ ;
2.  $x_L^*$  is monotonically increasing in  $\beta$  and  $\alpha_L$  and independent of  $\bar{\theta}$  and  $k$ ;
3.  $e_H^*$  is monotonically increasing in  $\bar{\theta}$ , decreasing in  $k$  and  $\alpha_L$  and independent of  $\beta$ ;
4.  $x_H^*$  is monotonically increasing in  $\beta$ , decreasing in  $\alpha_L$  and independent of  $\bar{\theta}$  and  $k$ ;
5.  $E^{T*} = e_H^*x_H^* + e_L^*x_L^*$  is monotonically increasing in  $\beta$  and  $\bar{\theta}$  and decreasing in  $k$  and  $\alpha_L$ .

*Proof.* Note that if  $\beta > 0$ ,  $\bar{\theta} > 0$ ,  $\alpha_H = 1$  and  $\alpha_L \in [0, 1)$  then the solution of the system identifies the following equilibrium levels of marginal abatement:

$$e_L^* = \frac{2(2 - \alpha_L)}{9 - 8\alpha_L + 2\alpha_L^2} \frac{\bar{\theta}}{k}; \quad (33)$$

$$e_H^* = \frac{2(2 - \alpha_L)^2}{9 - 8\alpha_L + 2\alpha_L^2} \frac{\bar{\theta}}{k}. \quad (34)$$

Substituting these solutions in equations (27) and (26) the following equilibrium market shares are achieved:

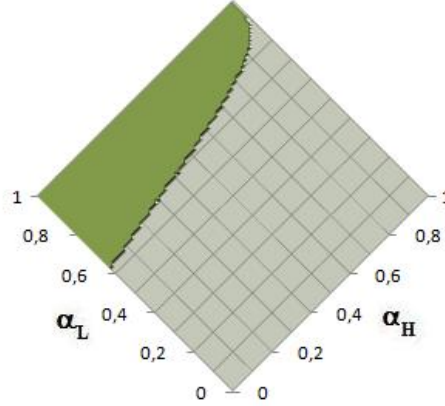
$$x_L^* = \frac{\beta(2 - \alpha_L)}{9 - 8\alpha_L + 2\alpha_L^2} \quad (35)$$

$$x_H^* = \frac{\beta(2 - \alpha_L)^2}{9 - 8\alpha_L + 2\alpha_L^2} \quad (36)$$

It is straightforward to check that parameters  $\beta$ ,  $\bar{\theta}$  and  $k$  affect  $e_L^*$ ,  $x_L^*$ ,  $e_H^*$ ,  $x_H^*$  and  $E^{T*}$  in the way stated in the proposition. As far as the impact of the the degree of CSR of the low-quality firm on firms' marginal abatement choices and on their market shares, the results stated in the proposition stem from the following derivatives:  $\frac{\partial e_L^*}{\partial \alpha_L} = \frac{2\bar{\theta}}{\beta k} \frac{\partial x_L^*}{\alpha_L} > 0$ ;  $\frac{\partial x_L^*}{\partial \alpha_L} = \beta \frac{2\alpha_L^2 - 8\alpha_L + 7}{(9 - 8\alpha_L + 2\alpha_L^2)^2} > 0$ ;  $\frac{\partial e_H^*}{\partial \alpha_L} = \frac{2\bar{\theta}}{\beta k} \frac{\partial x_H^*}{\alpha_L} < 0$ ;  $\frac{\partial x_H^*}{\partial \alpha_L} = -\beta \frac{2(2 - \alpha_L)}{(9 - 8\alpha_L + 2\alpha_L^2)^2} < 0$ ;  $\frac{\partial E^{T*}}{\partial \alpha_L} = \frac{4\beta\bar{\theta}}{2k} \frac{2\alpha_L - 4}{(9 - 8\alpha_L + 2\alpha_L^2)^4} < 0$ .  $\square$

Therefore, in the presence of a non-profit firm, the only Nash equilibrium is characterized by the fact that the other firm always adopts the lowest level of quality (i.e.: marginal abatement). Moreover, if this low quality firm assigns a higher weight to its CSR then its positive externality increases. However, this effect is counterbalanced by the reduction of the positive externality of the high quality firm. This result is coherent with the slope of the best response function of firm  $H$ . If firm  $L$  becomes more careful with the environmental impact of its production, it will increase its level of abatement, but at the same time, it will reduce its mark-up, increasing its supply. On the other hand, firm  $H$  cannot reduce its price without reducing its level of clean-up because it always charges a price equal to its marginal costs. Hence, firm  $H$  finds it convenient to decrease its level of abatement in order to limit the reduction of its market share. The last statement shows us that the aggregate effect of an increase in  $\alpha_L$  entails a reduction of the total abatement.

Figure 5: Nash equilibrium existence



More general results regarding the market equilibrium in the presence of two responsible firms can be obtained through numerical calculations. Figure 5 generalizes Proposition 3 identifying in the shaded region the set of couples  $(\alpha_H, \alpha_L)$  in which a Nash equilibrium (in pure strategies) fails to exist. Indeed, in such cases, firm  $H$  would have an incentive to leapfrog<sup>18</sup> firm  $L$  by choosing a level of abatement lower than  $e_L^*(\alpha_H, \alpha_L)$  in order to increase its market share and its total abatement. Consequently, at the first stage we can have zero, one or two Nash equilibria, depending on the weight that both the responsible firms assign to their profit. Making the symmetry of the shaded region with respect to the bisectrix we can identify three different regions: when the shaded region and its symmetric region coincide no Nash equilibrium exists. For all the other couples of values of  $(\alpha_i, \alpha_j)$  contained in the shaded region only a Nash equilibrium exists, in which  $\alpha_H > \alpha_L$ . Finally, for the couples of  $(\alpha_i, \alpha_j)$  which are contained nor in the shaded region nor in its symmetric counterpart, two Nash equilibria exist.

Hence, if both the firms assign a high weight to the positive externality associated to their own production, the outcome of their strategic interaction is unpredictable. However, when a Nash equilibrium exists, we can analyze through numerical calculations how the market equilibrium is affected by consumers' and firms' degree of responsibility. It is possible to verify that both  $e_L^*$  and  $e_H^*$  are linearly increasing in  $\frac{\bar{\theta}}{k}$  and independent of  $\beta$ , while both  $x_L^*$  and  $x_H^*$  are linearly increasing in  $\beta$  and independent of  $\bar{\theta}$  and  $k$ . As far as the impact of firms' degree

<sup>18</sup>The numerical calculations are available upon request.



of responsibility on market equilibrium we resume the main observations in the following lemma:

**Lemma 4.** *When a Nash equilibrium exists, the following properties hold:*

1.  $e_L^*$  is monotonically increasing in  $\alpha_L$ , while it is increasing (decreasing) in  $\alpha_H$  only when  $\alpha_L$  is sufficiently low (high). For intermediate values of  $\alpha_L$ ,  $e_L^*$  is (almost) constant.  $x_L^*$  is monotone increasing in  $\alpha_L$  and monotone decreasing in  $\alpha_H$ . Finally,  $e_L^*x_L^*$  is monotone increasing in  $\alpha_L$  and monotone decreasing in  $\alpha_H$ .
2.  $e_H^*$  is monotonically increasing (decreasing) in  $\alpha_H$  only when  $\alpha_L$  is sufficiently low (high). For intermediate values of  $\alpha_L$ ,  $e_H^*$  is at first increasing and then decreasing. At the same time,  $e_H^*$  is monotonically increasing (decreasing) in  $\alpha_L$  only when  $\alpha_H$  is sufficiently low (high). For intermediate values of  $\alpha_H$ ,  $e_H^*$  is at first decreasing and then increasing.  $x_H^*$  is monotone increasing in  $\alpha_H$  and monotone decreasing in  $\alpha_L$ . Finally,  $e_H^*x_H^*$  is monotone increasing in  $\alpha_H$  and monotone decreasing in  $\alpha_L$ .
3.  $E^{T*} = e_H^*x_H^* + e_L^*x_L^*$  is monotone increasing (decreasing) in  $\alpha_H$  if  $\alpha_L$  is sufficiently low (high) and monotone increasing (decreasing) in  $\alpha_L$  if  $\alpha_H$  is sufficiently low (high).
4.  $\lambda^* = e_H^*/e_L^*$  is always monotone decreasing in  $\alpha_L$  while it is monotone decreasing in  $\alpha_H$  only if  $\alpha_L$  is sufficiently high. When  $\alpha_L$  is low,  $\lambda^*$  is first increasing and then decreasing in  $\alpha_H$ .

*Proof.* See the 3D plots in Figure 6. □

Hence, we can observe that the equilibrium levels of per unit abatement are affected in different ways by firms' degree of responsibility. At the same time, firms' market shares and their total abatement are always increasing in their own degree of CSR, and decreasing in the degree of responsibility of the rival firm. The overall impact on the aggregate level of clean-up can be various. Indeed, an increase in the degree of responsibility of one firm can either increase or decrease the aggregate clean-up depending on the degree of responsibility of the other firm. Finally, an increase in the degree of responsibility of firm  $L$  makes the allocation of the abatement activity more cost effective (i.e. it decreases the value of  $\lambda^*$ ), while an increase in the degree of responsibility of firm  $H$  has not always the same effect on  $\lambda^*$ .

**Lemma 5.** *When an equilibrium exists,  $e_H^* \leq e^{FB}$  and  $e_L^* \leq e^{FB}$ , depending on the specific values of  $\bar{\theta}, \alpha_L, \alpha_H$ . At the same time,  $\rho^T - \frac{k}{2}e_i^* > 0, \forall i = L, H, \forall \bar{\theta}, \alpha_L, \alpha_H$ .*

*Proof.* See the graph of  $e_H^*$  and  $e_L^*$  in Figure 6. When  $\beta, \bar{\theta}$  and  $k$  are put equal to 1, there are couples  $(\alpha_H, \alpha_L)$  for which  $e_H^*$  and/or  $e_L^*$  are higher than 0.5. As a consequence, given the linear proportionality to  $\bar{\theta}$ , when maximum consumers' WTP is close to its maximum value (i.e.  $2\rho^T$ ) both the responsible firms may exert a level of abatement higher than the first best level (i.e.  $\frac{\rho^T}{k}$ ). At the same time, the graph of  $e_H^*$  and  $e_L^*$  in Figure 6 show that both the equilibrium levels of clean-up never assume a value higher than  $\frac{\bar{\theta}}{k}$ . Hence, the inequality contained in the lemma follows.  $\square$

Therefore, contrarily to what happens in the fixed costs case, when the costs are variable in equilibrium both firms may choose to exert a level of abatement inefficiently high (i.e. higher than the first best level). Hence, the statements of Lemma 4 and 5 do not allow any clear deduction with regard to the influence on the social welfare of a higher degree of responsibility by part of consumers or of a single firm. Indeed, a higher degree of responsibility in the population of green consumers always increases the aggregate abatement, but it may induce the responsible firms to adopt an inefficiently high level of marginal abatement. At the same time, an increase in the degree of CSR of one firm has not a clear-cut effect on the aggregate abatement and on the cost-effectiveness of the allocation of such activity. We then devote next paragraph to the analysis of how the responsibility of consumers and firms affect the social welfare.

## 4.2 The Social Welfare

In the case of variable costs of clean-up, the social welfare defined in equation (3) can be rewritten as:

$$W = \sum_{i=H,L} \left[ \rho^T e_i^* - \frac{k}{2} (e_i^*)^2 \right] x_i^*. \quad (37)$$

**Proposition 4.** *The social welfare function is monotone increasing in  $\beta$  and concave in  $\bar{\theta}$  (i.e.:  $\frac{\partial^2 W}{\partial \bar{\theta}^2} < 0$ ). Its partial (first) derivative with respect to  $\bar{\theta}$  is never monotone.*

*Proof.* In this case the variation of  $W$  with respect to a generic exogenous parameter  $z$  is:

$$\frac{\partial W}{\partial z} = \sum_{i=H,L} \left[ (\rho^T - ke_i^*)x_i^* \frac{\partial e_i^*}{\partial z} + (\rho^T - \frac{k}{2}e_i^*)e_i^* \frac{\partial x_i^*}{\partial z} \right].$$

Consequently,  $\frac{\partial W}{\partial \beta}$  is surely positive given that  $\frac{\partial e_i^*}{\partial \beta} = 0$ ,  $(\rho^T - \frac{k}{2}e_i^*) > 0$  (see Lemma 5) and  $\frac{\partial x_i^*}{\partial \beta} > 0$ ,  $\forall i = L, H$ .

Given that  $\frac{\partial x_i^*}{\partial \theta} = 0$  and  $\frac{\partial^2 e_i^*}{\partial \theta^2} = 0$  we obtain that:

$$\frac{\partial^2 W}{\partial \theta^2} = -k \sum_{i=H,L} x_i^* \left( \frac{\partial e_i}{\partial \theta} \right)^2 < 0$$

Hence,  $W$  is concave in  $\bar{\theta}$ . Furthermore, as  $\frac{\partial e_i^*}{\partial \theta} > 0$  and  $\frac{\partial x_i^*}{\partial \theta} = 0$ , we can note that the sign of  $\frac{\partial W}{\partial \theta}$  depends on the sign of  $(\rho^T - ke_i^*)$ ,  $\forall i = L, H$ . Consequently, when  $\bar{\theta}$  is close to 0 ( $2\rho^T$ ) both  $e_H^*$  and  $e_L^*$  are lower (higher) than  $e^{FB}$  and  $W$  is increasing (decreasing) in  $\bar{\theta}$ . Therefore,  $W$  is never monotone in  $\bar{\theta}$ .  $\square$

As far as the pattern of  $W$  with respect to  $\alpha_L$  and  $\alpha_H$ , it is impossible to derive analytical results. However, using numerical simulations, in Figure 7 we show that  $W$  can be both increasing and decreasing in firms' degree of responsibility, depending on the specific values of  $\alpha_L$ ,  $\alpha_H$  and  $\bar{\theta}$ .

Therefore, in the variable costs case, the impact of  $\alpha_H$  and  $\alpha_L$  on the social welfare depends crucially on their values and on the value of  $\bar{\theta}$ . In some cases a higher degree of responsibility of one firm can harm the social welfare. For instance, the social welfare turn out to be monotonically decreasing in  $\alpha_L$  when  $\alpha_H$  is very high and  $\bar{\theta}$  is very low. At the same time, the social welfare is monotonically decreasing in  $\alpha_H$  when  $\alpha_L$  is very low and  $\bar{\theta}$  is very high.

Three relevant results regarding the link between firms' degree of responsibility and the social welfare attained in equilibrium are emphasized in the following propositions:

**Proposition 5.** *The highest social welfare is attained when  $\beta = 1$ ,  $\bar{\theta} \simeq 1,463\rho^T$ ,  $\alpha_H = 1$  and  $\alpha_L \simeq 0,85$ , and it does not correspond to the first best solution.*

*Proof.* The maximum of  $W$  can be obtained through numerical calculations. In correspondence of such values  $W = 0.33783 \frac{(\rho^T)^2}{k}$ . If all the existing firms could adopt a level of abatement equal to the first best level the social welfare would

be equal to  $0.5 \frac{(\rho^T)^2}{k}$ . Therefore, when the abatement cost are explicitly linked to sales, the maximum social welfare achievable in equilibrium is only the 0,67% of its first best level.  $\square$

**Proposition 6.** *If  $\bar{\theta}$  is very high then social welfare is higher in a standard duopoly than in a mixed duopoly.*

*Proof.* Thanks to Figure 5 we know that in the presence of a non-profit firm and of a profit-maximizing only a Nash equilibrium exists, in which the former chooses the high level of abatement and the latter the low level. Observing the third graph in Figure 7 we can note that when  $\bar{\theta}$  is very high,  $W(0, 0) > W(1, 0)$ . Therefore social welfare is higher in a standard duopoly (i.e. in the presence of two profit-maximizing firms) than in a mixed duopoly (i.e. in the presence a non-profit firm and a profit-maximizing firm)  $\square$

**Proposition 7.** *Assume that  $\alpha_H = \alpha'_L > \alpha_L = \alpha'_H$ . There are cases in which  $W(\alpha_H, \alpha_L) < W(\alpha'_H, \alpha'_L)$ .*

*Proof.* Observing the third graph in Figure 7 we can note that when  $\bar{\theta}$  is very high, the social welfare in  $W(0, 0)$  is decreasing in  $\alpha_H$  and increasing in  $\alpha_L$ . As a consequence,  $W(y, 0) < W(0, y)$  for any  $y$  strictly positive and close to 0.  $\square$

Hence, when the abatement costs are proportional to firms' sales the conclusions are quite more confusing than in the fixed costs case. First of all, a higher degree of responsibility of consumers' and/or firms may decrease the social welfare. Moreover, the presence of a no-profit firm competing with a profit-maximizing firm may harm social welfare. Consequently is not always reasonable for consumers and share-holders to sacrifice their private utility in order to voluntarily contribute to the environmental protection. Finally, when two Nash equilibria exists, there are cases in which the social welfare is higher when the more responsible firm produces the low (environmental) quality good. Therefore in such cases the firm with some degree of altruism should choose a level of abatement lower than its profit-maximizing rival.

## 5 Conclusions

In this paper we investigate how the market equilibrium is affected by the presence of green consumers and responsible firms. We have introduced a model where some consumers care about the environmental impact of goods they buy and some

firms, following a multidimensional objective, weigh together the maximization of both their profit and their abatement activity. Our analysis has focused mainly on the effects associated to exogenous minor changes in aggregate consumers' willingness to pay for cleaner goods or in the degree of firms' social responsibility.

In accordance with the existing literature, we have found that the presence of green consumers is sufficient to induce some firms to overcomply the minimum environmental standard. However we have also shown that green consumers are also necessary. Indeed, even if firms want to maximize their abatement effort, they would be forced to employ the standard technology if in the market nobody is willing to pay an extra-premium for their environment friendly products.

A second result is that in our model the nature of the abatement cost function influences how a higher level of responsibility of both producers and consumers affects the efficiency of aggregate clean-up. If the costs of the cleaning process are fixed, then social welfare is monotone increasing in consumers' WTP and in firms' CSR. On the other hand, if the abatement costs are variable, social welfare may be reduced by an increase of consumers' WTP and by a higher degree of firms' CSR. Therefore we cannot take for granted that a higher responsibility is associated to a higher welfare. Moreover, if the abatement costs are fixed social welfare is always higher in a mixed than in a standard duopoly. Conversely, when the costs are variable, social welfare may be reduced by the presence of a non-profit firm.

Finally, we have found that in both cases, a full responsibility of consumers and producers is sufficient neither to implement the first best level of aggregate clean-up, nor to achieve a cost effective allocation of the abatement activity. Hence, the existence of individuals who take care of the environment in their market decisions is usually a good news, but it cannot be considered a perfect substitute for environmental regulation.

Future research should extend our analysis in order to check the robustness of our results under different assumptions. For instance, firms could compete in a different market form: we could assume that one firm is a Stackelberg leader, and/or that the number of responsible firms is endogenous. Moreover, responsible firms could maximize other kind of objective functions. Finally, firms' degree of CSR could be endogenous: in such case we should analyze the dynamic properties of the interaction between green consumers and responsible firms.

## 6 Technical Appendix

In this appendix we want to prove that at each stage the pair of candidate equilibrium prices or qualities (i.e. the solutions of the system given by the first order conditions stemming from firms' maximization problems) represents a Nash equilibrium. For this purpose we need to show that i) second order conditions are satisfied, and that ii) the low (high) quality firm has no incentive to leapfrog its rival by choosing a level of abatement higher than  $e_H^*$  (lower than  $e_L^*$ ).

We start by introducing the following lemma: let  $J_i$  be an objective function given by the weighted product of two different functions:  $J_i = [\pi_i(z_i)]^{1-\alpha_i} [E_i(z_i)]^{\alpha_i}$

**Lemma 6.** *If both  $\pi_i$  and  $E_i$  are log-concave in  $z_i$ , then the solution of the first order condition,  $z_i^*$ , represents a local maximum.*

*Proof.* We recall that the solution of a maximization problem is invariant wrt monotone transformation of the objective function, so:

$$\begin{aligned} \max_{z_i} [\pi_i(z_i)]^{1-\alpha_i} [E_i(z_i)]^{\alpha_i} &\equiv \max_{z_i} \log [\pi_i(z_i)]^{1-\alpha_i} [E_i(z_i)]^{\alpha_i} \equiv \\ &\equiv \max_{z_i} (1 - \alpha_i) \log [\pi_i(z_i)] + \alpha_i \log [E_i(z_i)] \end{aligned}$$

Hence, if both  $\pi_i$  and  $E_i$  are log-concave in  $z_i$ , then the second order condition of the maximization problem holds.  $\square$

**Proposition 8.** *At each stage the solutions of first order conditions represent always local maxima.*

*Proof.* In order to guarantee that the solution of each first order condition is indeed a local maximum we need to prove that second order conditions always hold. Thanks to Lemma 6 we have to show that at each stage the profit and the positive externality are log-concave in each firm's strategic choice.

As far as the fixed costs case is concerned, we know from the existing literature (see for instance Arora and Gangopadhyay, 1995) that each firm's profit function is concave in firm's price strategy at the second stage (whatever the quality equilibrium) and in each firm's quality choice at the first stage. However, concavity of the profit functions imply also their log-concavity. At the same time, the positive externality of each firm is equal to  $e_i$  which is obviously log-concave in itself.

With regard to the variable costs case, the log-concavity of firms' objective function is shown below.

- *Price stage* - Using formulas (23) and (9) we obtain:

$$\begin{aligned}\frac{\partial^2 \log[\pi_H]}{\partial p_H^2} &= \frac{\partial^2 \log(p_H - \frac{k}{2}e_H^2)}{\partial p_H^2} + \frac{\partial^2 \log x_H}{\partial p_H^2}; \\ &= -\frac{1}{(p_H - \frac{k}{2}e_H^2)^2} - \frac{1}{(\bar{\theta}(e_H - e_L) - p_H + p_L)^2} < 0. \\ \frac{\partial^2 \log[e_H x_H]}{\partial p_H^2} &= -\frac{1}{(\bar{\theta}(e_H - e_L) - p_H + p_L)^2} < 0.\end{aligned}$$

$$\begin{aligned}\frac{\partial^2 \log[\pi_L]}{\partial p_L^2} &= \frac{\partial^2 \log(p_L - \frac{k}{2}e_L^2)}{\partial p_L^2} + \frac{\partial^2 \log x_L}{\partial p_L^2}; \\ &= -\frac{1}{(p_L - \frac{k}{2}e_L^2)^2} - \frac{e_H^2}{(p_H e_L - p_L e_H)^2} < 0. \\ \frac{\partial^2 \log[e_L x_L]}{\partial p_L^2} &= -\frac{e_H^2}{(p_H e_L - p_L e_H)^2} < 0.\end{aligned}$$

- *Quality stage* - Recalling formulas (24) and (25) we can write:

$$\log \pi_H = \log(1 - \alpha_H)(e_H - e_L) + 2 \log x_H;$$

$$\log \pi_L = \log(1 - \alpha_L)(e_H - e_L) + \log e_L - \log e_H + 2 \log x_L;$$

where, thanks to formulas (26) and (27) we can know that:

$$\begin{aligned}\log x_H &= \log \beta e_H + \log [(2 - \alpha_L)(2\bar{\theta} - ke_H) - ke_L] - \\ &\quad - \log 2\bar{\theta}[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L];\end{aligned}$$

$$\begin{aligned}\log x_L &= \log \beta e_H + \log [(1 - \alpha_H)(2\bar{\theta} - ke_L) + ke_H] - \\ &\quad - \log 2\bar{\theta}[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L];\end{aligned}$$

Consequently we can calculate the following derivatives:

$$\begin{aligned}\frac{\partial^2 \log[\pi_H]}{\partial e_H^2} &= -\frac{1}{(e_H - e_L)^2} - \frac{1}{e_H^2} - 2\frac{[(2 - \alpha_L)k]^2}{[(2 - \alpha_L)(2\bar{\theta} - ke_H) - ke_L]^2} - \\ &\quad - 2\frac{[(2 - \alpha_H)(2 - \alpha_L)]^2}{[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]^2} < 0;\end{aligned}$$

$$\begin{aligned} \frac{\partial^2 \log[\pi_L]}{\partial e_L^2} = & -\frac{1}{(e_H - e_L)^2} - \frac{1}{e_L^2} - 2 \frac{[(1 - \alpha_H)k]^2}{[(1 - \alpha_H)(2\bar{\theta} - ke_L) + ke_H]^2} - \\ & - 2 \frac{[(2 - \alpha_H)(2 - \alpha_L)]^2}{[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]^2} < 0; \end{aligned}$$

$$\begin{aligned} \frac{\partial^2 \log[e_H x_H]}{\partial e_H^2} = & -\frac{2}{e_H^2} - 2 \frac{[(2 - \alpha_L)k]^2}{[(2 - \alpha_L)(2\bar{\theta} - ke_H) - ke_L]^2} - \\ & - 2 \frac{[(2 - \alpha_H)(2 - \alpha_L)]^2}{[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]^2} < 0; \end{aligned}$$

$$\begin{aligned} \frac{\partial^2 \log[e_L x_L]}{\partial e_L^2} = & -\frac{1}{e_L^2} - 2 \frac{[(1 - \alpha_H)k]^2}{[(1 - \alpha_H)(2\bar{\theta} - ke_L) + ke_H]^2} - \\ & - 2 \frac{[(2 - \alpha_H)(2 - \alpha_L)]^2}{[(2 - \alpha_H)(2 - \alpha_L)e_H - (1 - \alpha_H)(1 - \alpha_L)e_L]^2} < 0. \end{aligned}$$

□

Finally, in order to guarantee that  $(e_L^*, e_H^*)$  is indeed a Nash equilibrium we have to check that the firm choosing  $e_L^*$  has no incentive to "leapfrog" its rival by choosing a quality higher than  $e_H^*$ . Likewise, we have to verify that firm choosing the highest quality,  $e_H^*$ , has no incentive to deviate by producing a quality lower than  $e_L^*$ . Formally, we must check that:

$$J_L(e_L^*, e_H^*) > J_H(e_L^*, e_H^*) \quad \forall \alpha_H, \alpha_L \in [0, 1], \quad (38)$$

where  $e_1^*$  in the fixed costs case is the solution of equation (13) (for the variable costs case we have to consider equation (28)) when  $e_L = e_H^*$ , and:

$$J_H(e_H^*, e_L^*) > J_L(e_H^*, e_L^*), \quad \forall \alpha_H, \alpha_L \in [0, 1], \quad (39)$$

where  $e_2^*$  in the fixed costs case is the solution of equation 14 (for the variable costs case we have to consider equation (29)) when  $e_H = e_L^*$

From the numerical calculations we can observe that in the fixed costs case no firm has an incentive to leapfrog its rival in equilibrium. However, in the variable costs case, firm  $H$  has an incentive to leapfrog firm  $L$  when  $\alpha_L$  is sufficiently high and  $\alpha_H$  is sufficiently low (see Figure 5). The file with the numerical calculations is available upon request.



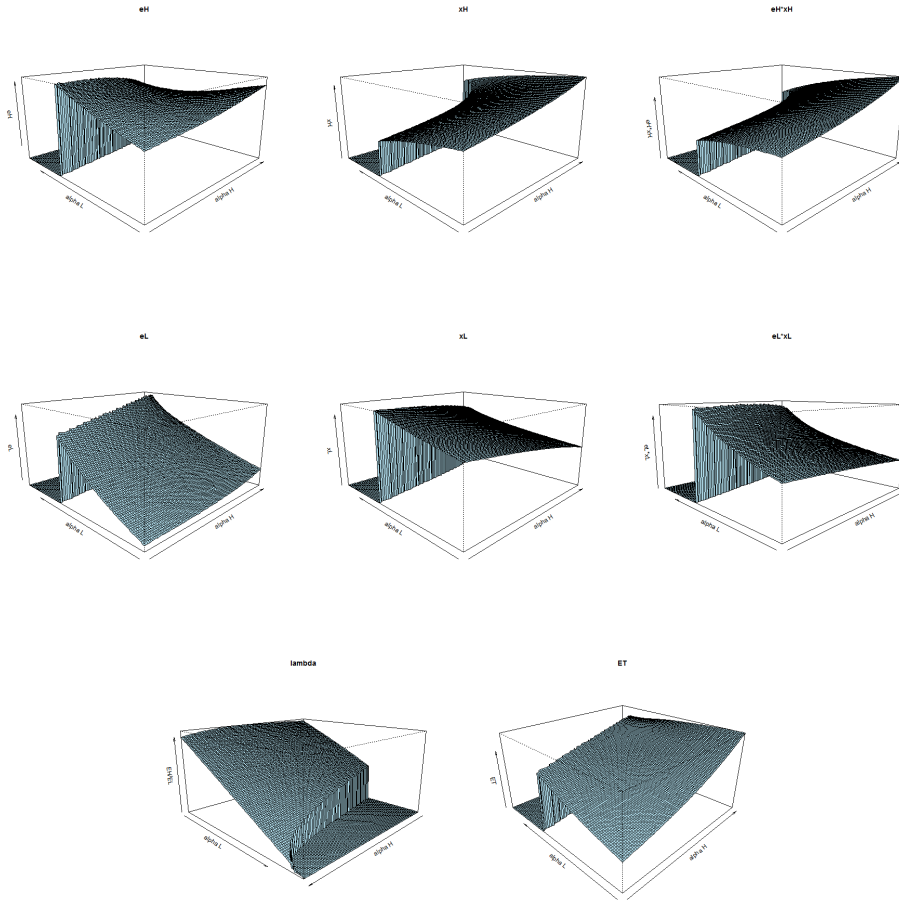
## References

- [1] Andreoni, J., 1990, "Impure Altruism and Donations to Public Goods: a Theory of Warm-glow Giving," *The Economic Journal*, 100, 464-477.
- [2] Arora, S. and S. Gangopadhyay, 1995, "Toward a Theoretical Model of Voluntary Overcompliance," *Journal of Economic Behavior and Organization*, 28, 289-309.
- [3] Bagnoli, M. and S.G. Watts, 2003, "Selling to Socially Responsible Consumers: Competition and the Private Provision of Public Goods," *Journal of Economics and Management Strategy* 12, 419-445.
- [4] Bansal, S. and S. Gangopadhyay, 2003, "Tax/subsidy Policies in the Presence of Environmentally Aware Consumers," *Journal of Environmental Economics and Management* 45, 333-355.
- [5] Baron, D.P., 2007, "Corporate Social Responsibility and Social Entrepreneurship," *Journal of Economics and Management Strategy*, 16, 683-717.
- [6] Becchetti, L. and B. Huybrechts, 2008, "The Dynamic of Fair Trade as a Mixed-form Market," *Journal of Business Ethics*, 81, 733-750.
- [7] Bénabou, R. and J. Tirole, 2010, "Individual and Corporate Social Responsibility," *Economica*, 77, 1-19.
- [8] Besley, T. and M. Ghatak, 2007, "Retailing Public Goods: the Economics of Corporate Social Responsibility," *Journal of Public Economics*, 91, 1645-1663.
- [9] Bulow, J.I., J.D. Geanakoplos and P.D. Klemperer, 1985, "Multimarket Oligopoly: Strategic Substitutes and Complements," *Journal of Political Economy*, 93, 488-511.
- [10] Calveras, A., J.J. Ganuza and G. Llobet, 2007, "Regulation, Corporate Social Responsibility and Activism," *Journal of Economics and Management Strategy*, 16, 719-740.
- [11] Conrad, K., 2005, "Price Competition and Product Differentiation When Consumers Care for the Environment," *Environmental and Resource Economics*, 31, 1-19.

- [12] Cremer, H. and J.F. Thisse, 1999, "On the Taxation of Polluting Products in a Differentiated Industry", *European Economic Review* 43, 575-594.
- [13] De Donder, P. and J.E. Roemer, 2009, "Mixed Oligopoly Equilibria when Firms' Objectives are Endogenous," *International Journal of Industrial Organization*, 27, 414-423.
- [14] Eriksson, C., 2004, "Can Green Consumerism Replace Environmental Regulation? A Differentiated-Products Examples," *Resource and Energy Economics*, 26, 281-293.
- [15] Garcia-Gallego, A. and N. Georgantzis, 2009, "Market Effects of Changes in Consumers' Social Responsibility," *Journal of Economics and Management Strategy*, 18, 235-262.
- [16] Khanna, M., 2001, "Non-Mandatory Approaches to Environmental Protection," *Journal of Economic Surveys*, 15, 291-324.
- [17] Kotchen, M.J., 2005, "Impure Public Goods and the Comparative Statics of Environmentally Friendly Consumption," *Journal of Environmental Economics and Management*, 49, 281-300.
- [18] Lombardini-Riipinen, C., 2005, "Optimal Tax Policy under Environmental Quality Competition," *Environmental and Resource Economics* 32, 317-336.
- [19] Lyon, T.P. and J.W. Maxwell, 2008, "Corporate Social Responsibility and the Environment: a Theoretical Perspective," *Review of Environmental Economics and Policy*, 1, 1-22.
- [20] Moorthy, S.K., 1988, "Product and Price Competition in a Duopoly," *Marketing Science*, 7, 141-168.
- [21] Moraga-Gonzalez, J. L. and N. Padron-Fumero, 2002, "Environmental Policy in a Green Market," *Environmental and Resource Economics*, 22, 419-447.
- [22] Motta, M., 1993, "Endogenous Quality Choice: Price vs. Quantity Competition," *Journal of Industrial Economics*, 41, 113-131.
- [23] Ostrom, E., 2000, "Collective Action and the Evolution of Social Norms," *The Journal of Economic Perspectives*, 14, 137-158.

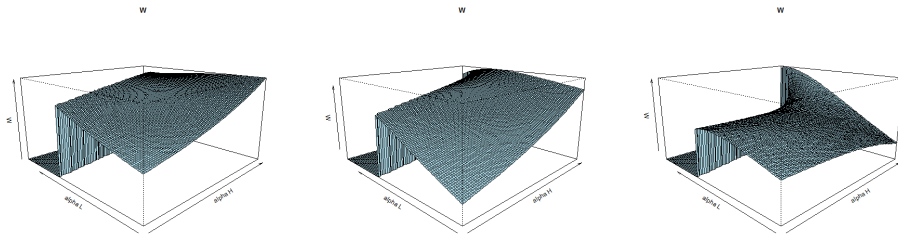
- [24] Reinhardt, F.L., R.N. Stavins and R.H.K. Vietor, 2008, "Corporate Social Responsibility through an Economic Lens," *Review of Environmental Economics and Policy*, 2, 219-239.
- [25] Rodriguez-Ibeas, R., 2007, "Environmental Product Differentiation and Environmental Awareness," *Environmental and Resource Economics*, 36, 237-254.

Figure 6: Illustration of Lemma 4



Figures are drawn assuming  $\bar{\theta} = 1$ ,  $k = 1$  and  $\beta = 1$ .

Figure 7:  $W(\alpha_H, \alpha_L)$



Social welfare pattern when  $\bar{\theta} = 0.2; 1; 1.8$ .

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